

# Determining causality in auditory pathways with TRENTool

Causality in source space:  
a FEM-aided MEG study

Dominic Portain  
Burkhard Maess  
A.D. Friederici

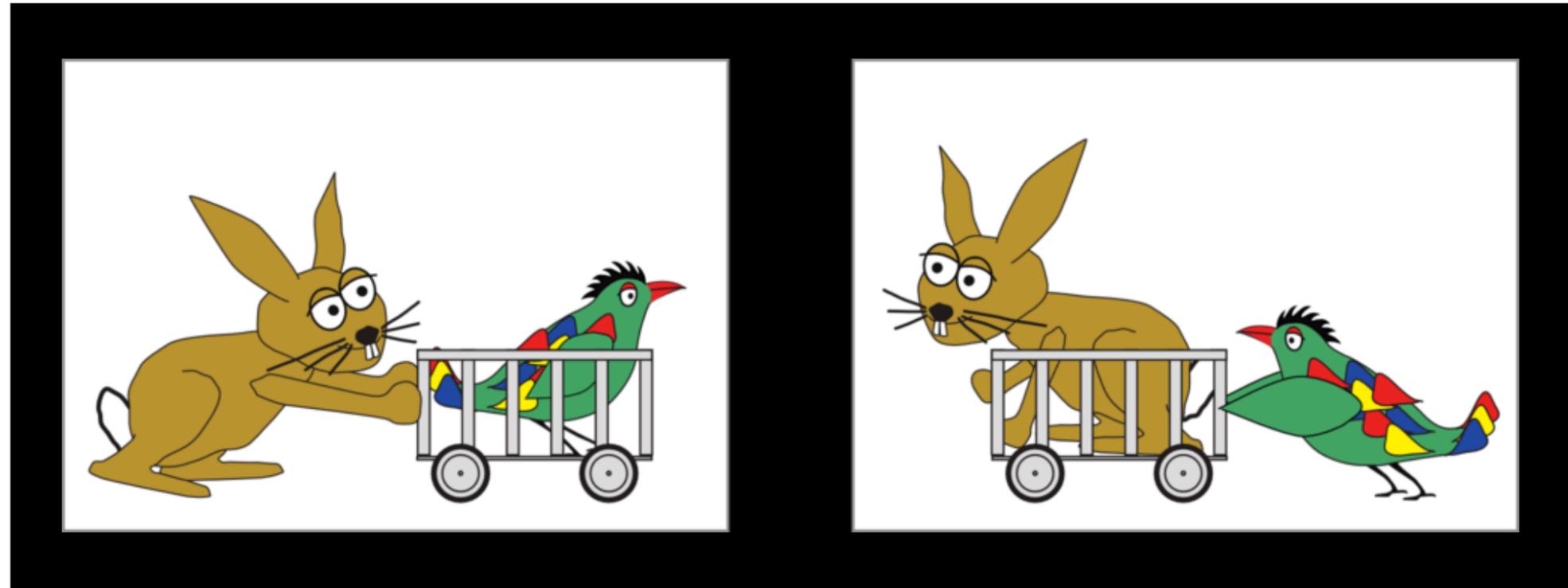
Max Planck Institute  
for Human Cognitive and Brain Sciences Leipzig, Germany

# Overview

- Task paradigm
- Cognitive background
- Data analysis
- Modeling Causality
- Transfer Entropy
- Properties of TRENTool

# Task

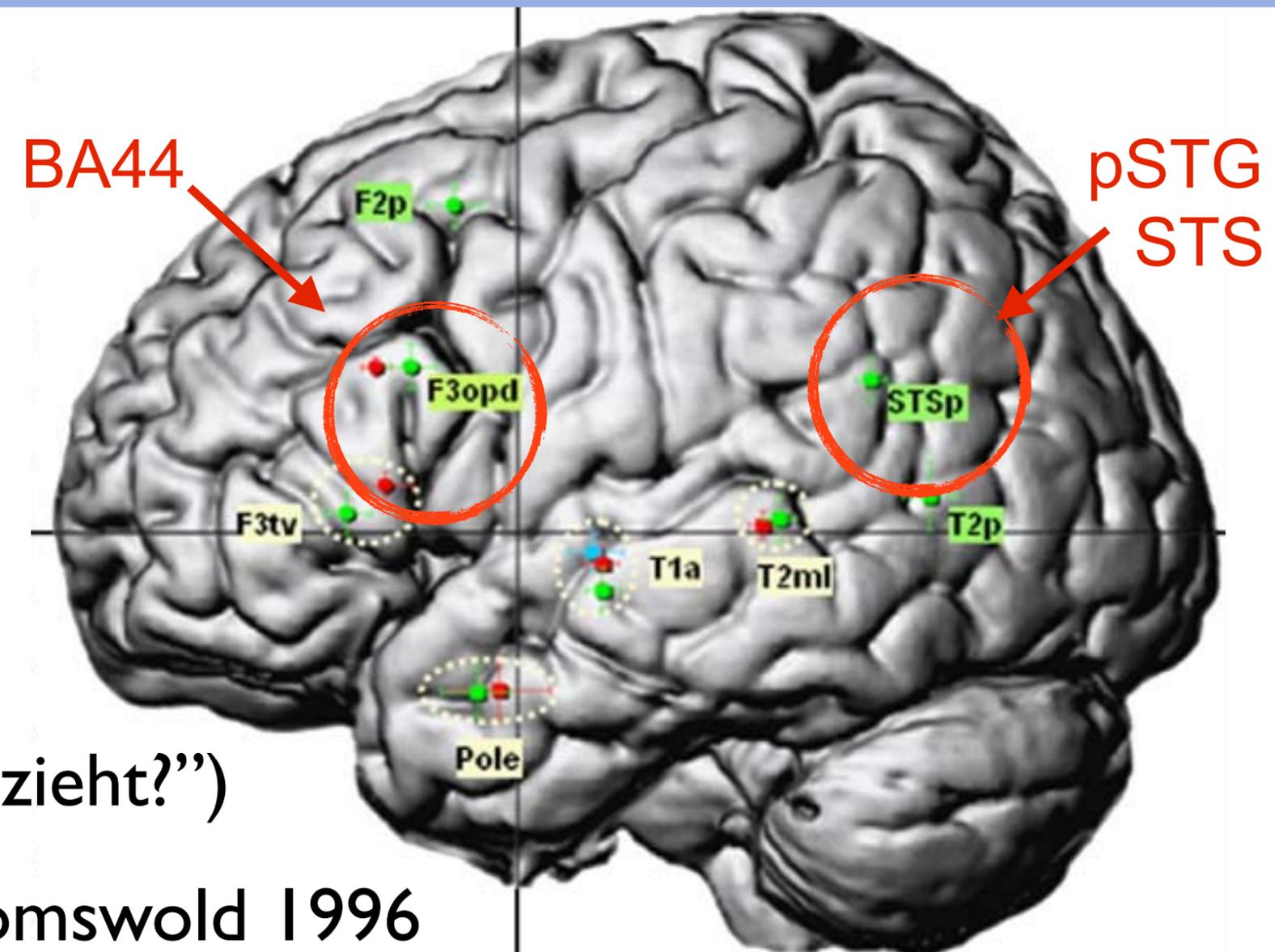
- Picture-Selection task
- 216 trials (Pilot, 18min)  
304 trials (MEG, 25min)
- Tutorial: random trials until 90% correct
- Feedback:
  - immediate: Correct response
  - delayed: Accuracy, Speed



“Wo ist das Tier, das **der** Vogel schiebt?”  
“Wo ist das Tier, das **den** Vogel schiebt?”

# Paradigm

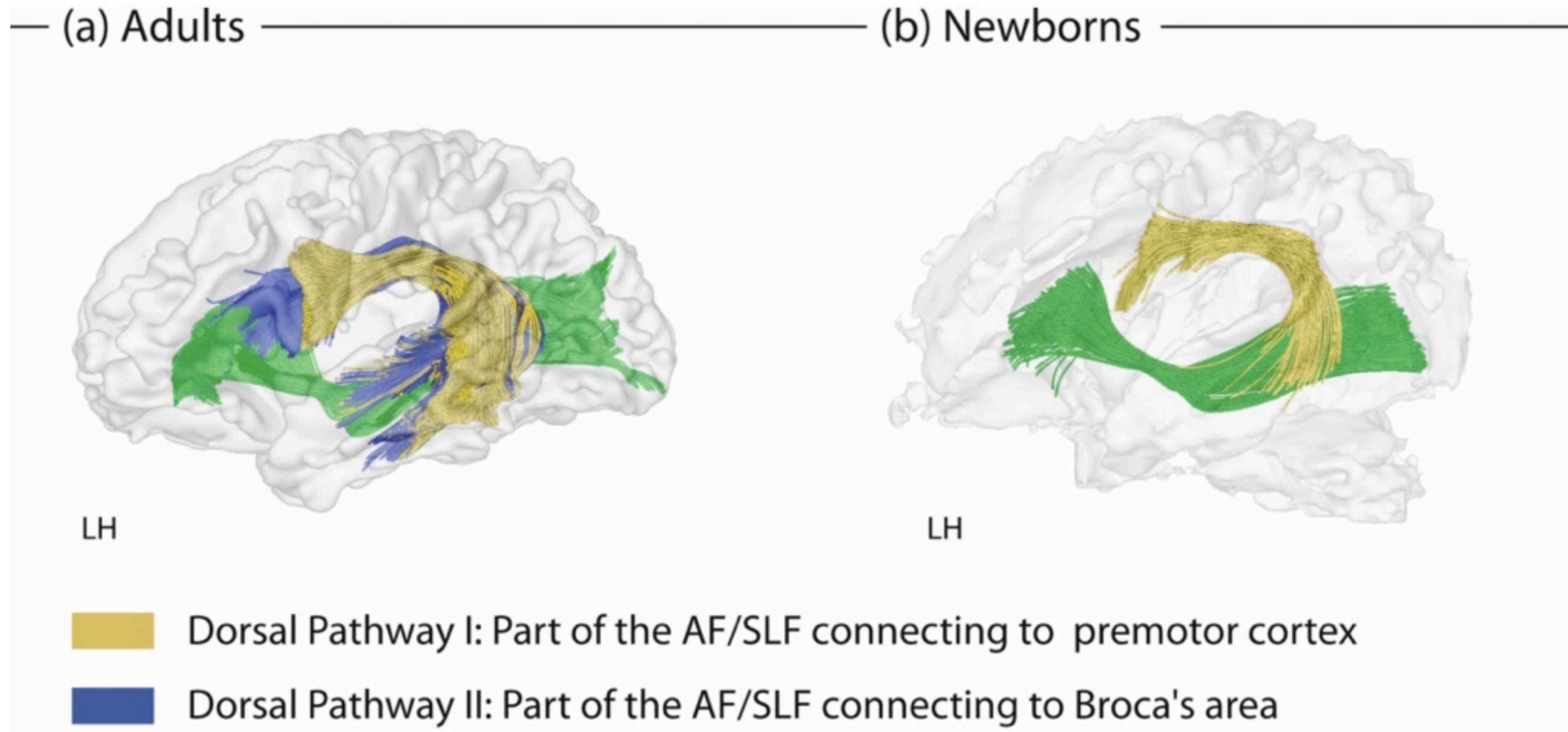
- “Subject-object” paradigm (“Wo ist der Affe, den der Tiger zieht?”)
- fMRI evidence: Cooke 2002, Stromswold 1996
- Activation in pSTG/STS during syntactic comprehension
- Contrast in BA44 between subject/object-first conditions



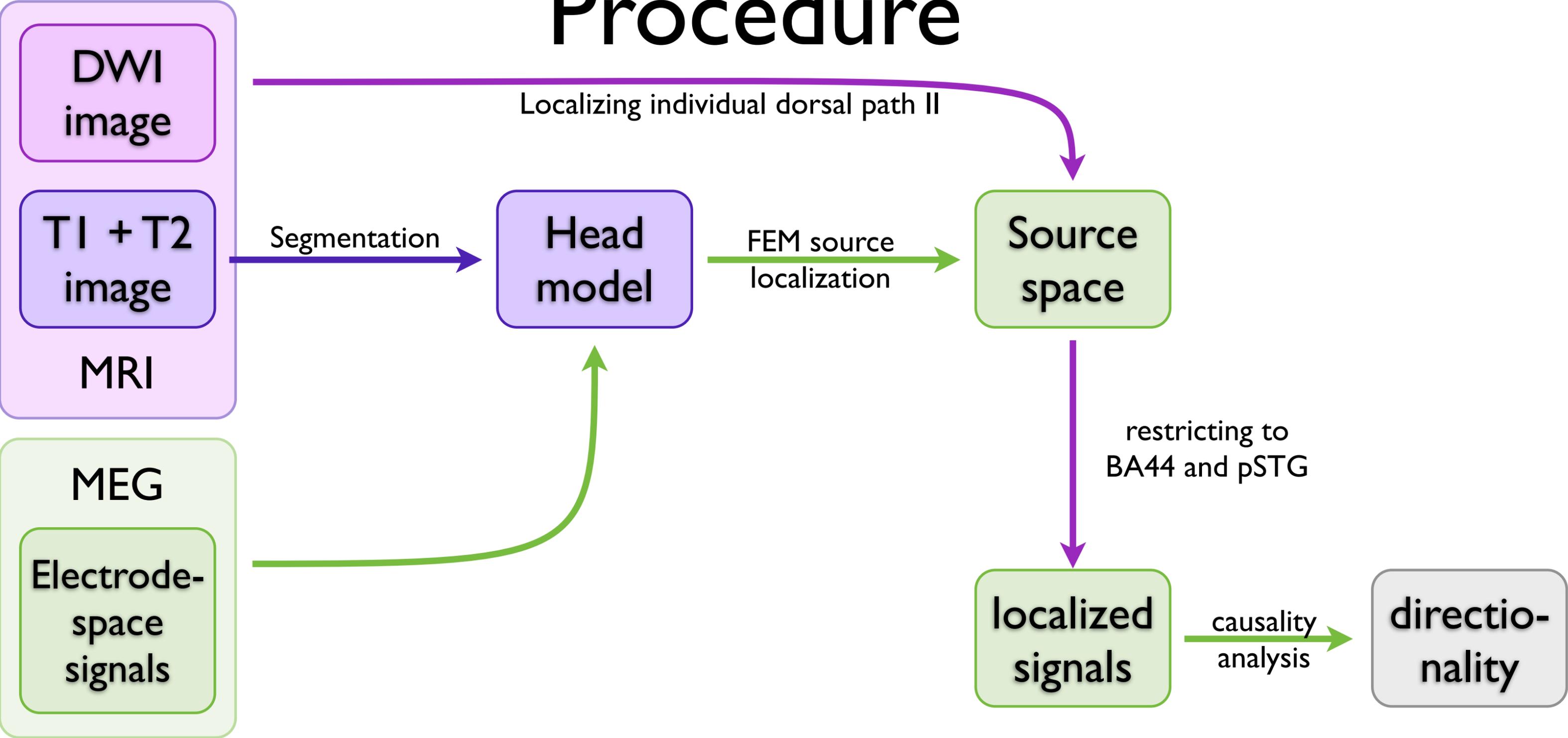
Vigneau 2006, NeuroImage

# Age influence

Perani et al., PNAS 2011

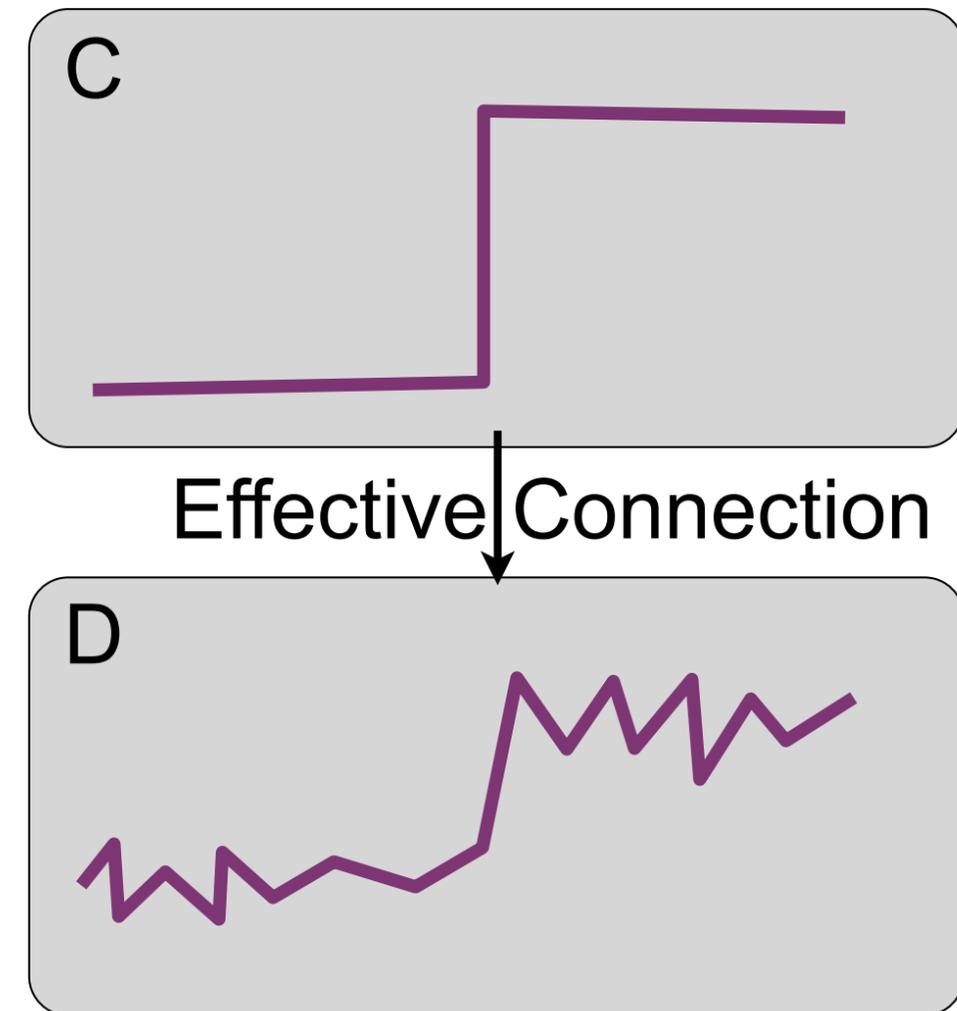
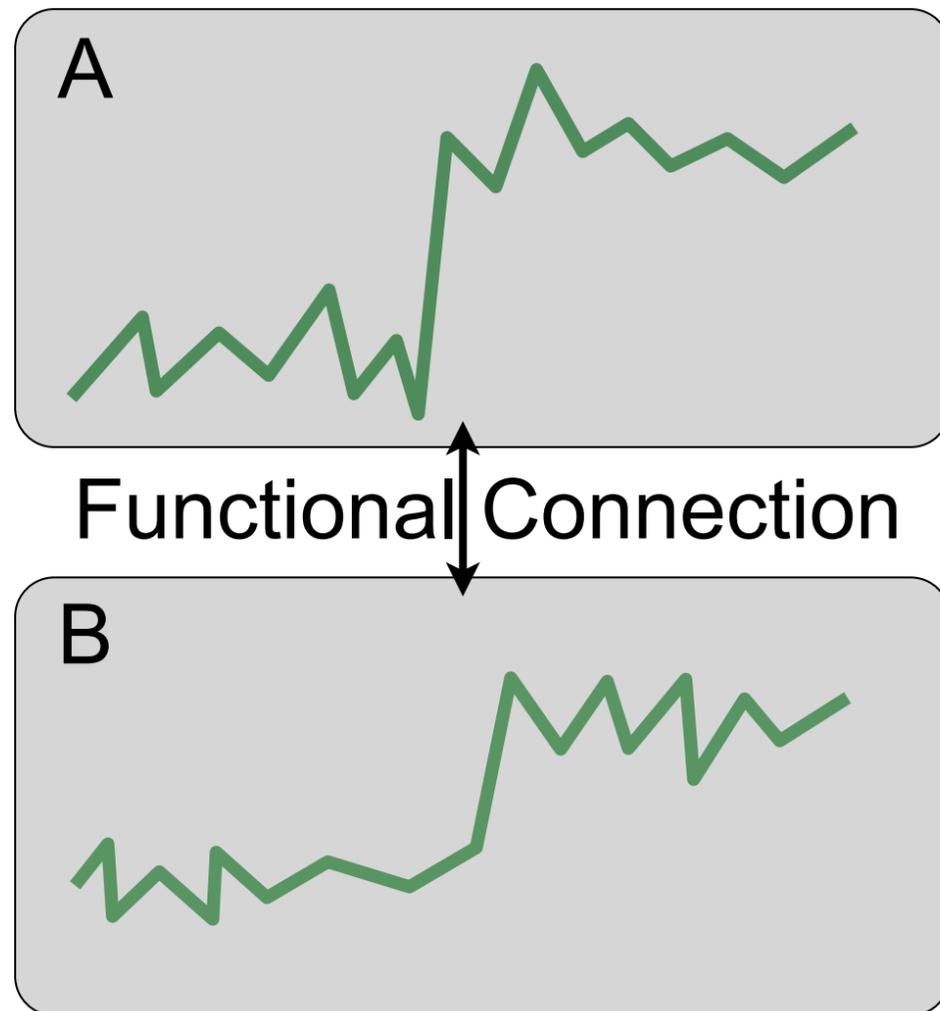


# Procedure



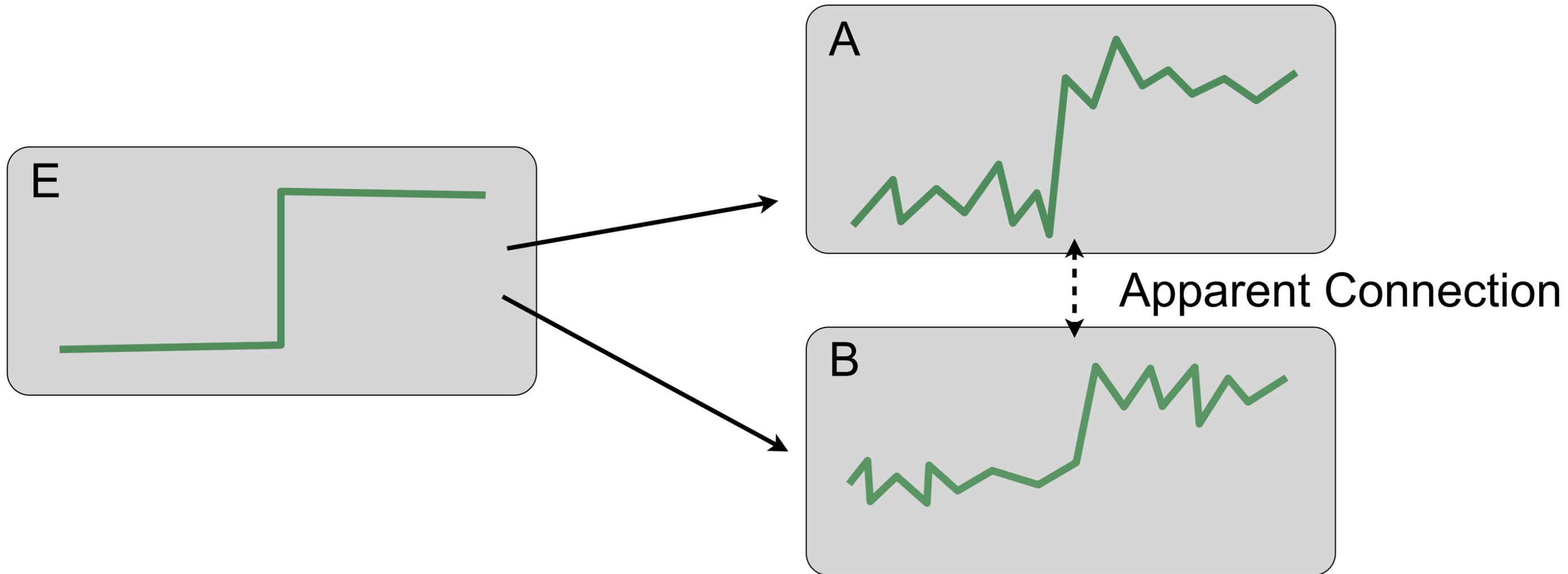
# Functional vs. effective causality

Discriminating cause and effect



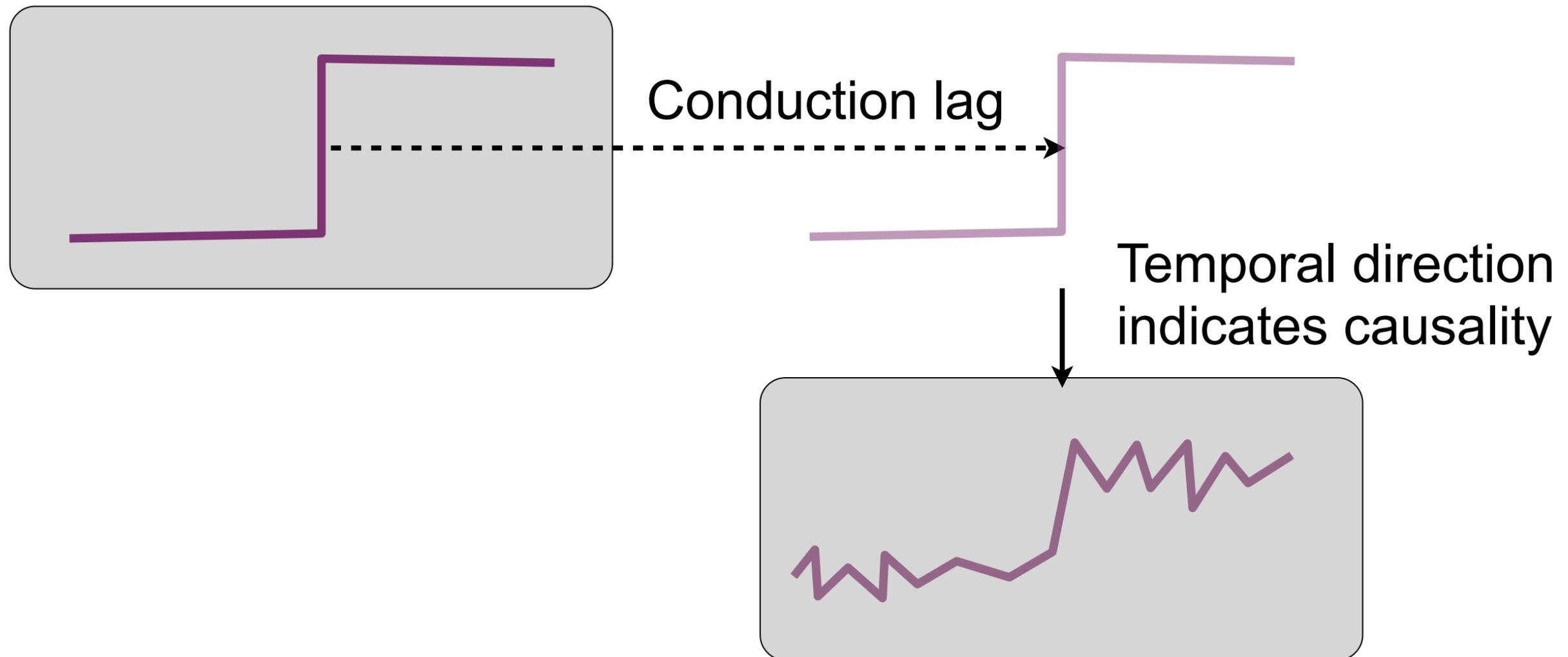
# Functional vs. effective causality

The pitfalls of functional causality



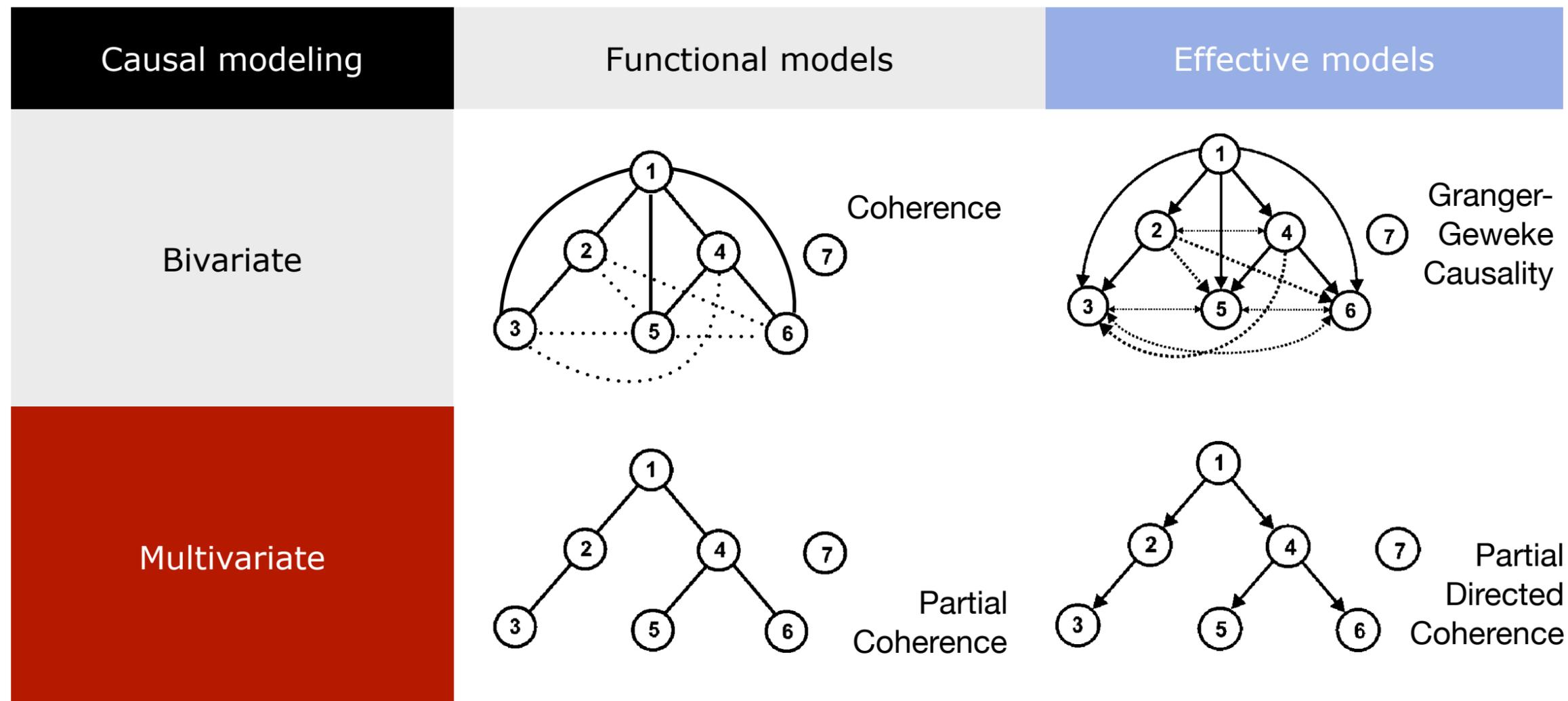
# Functional vs. effective causality

Effective Causality in cognitive Science



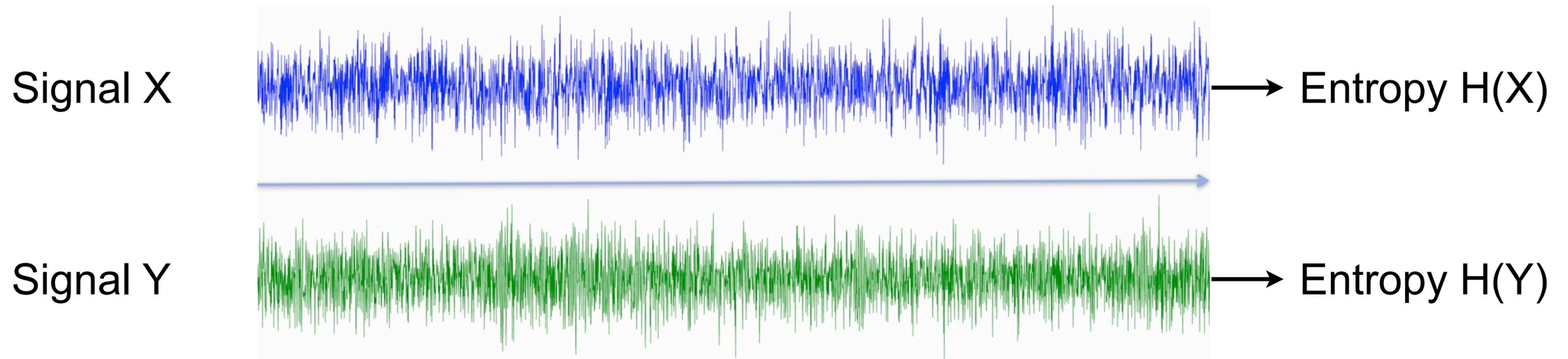
# Functional vs. effective causality

Causality methods



# Transfer Entropy

Entropy components



$$H(X) + H(Y) = H(X_{t+1}|X_t) + H(Y_{t+1}|Y_t) + I(X, Y)$$

Entropy

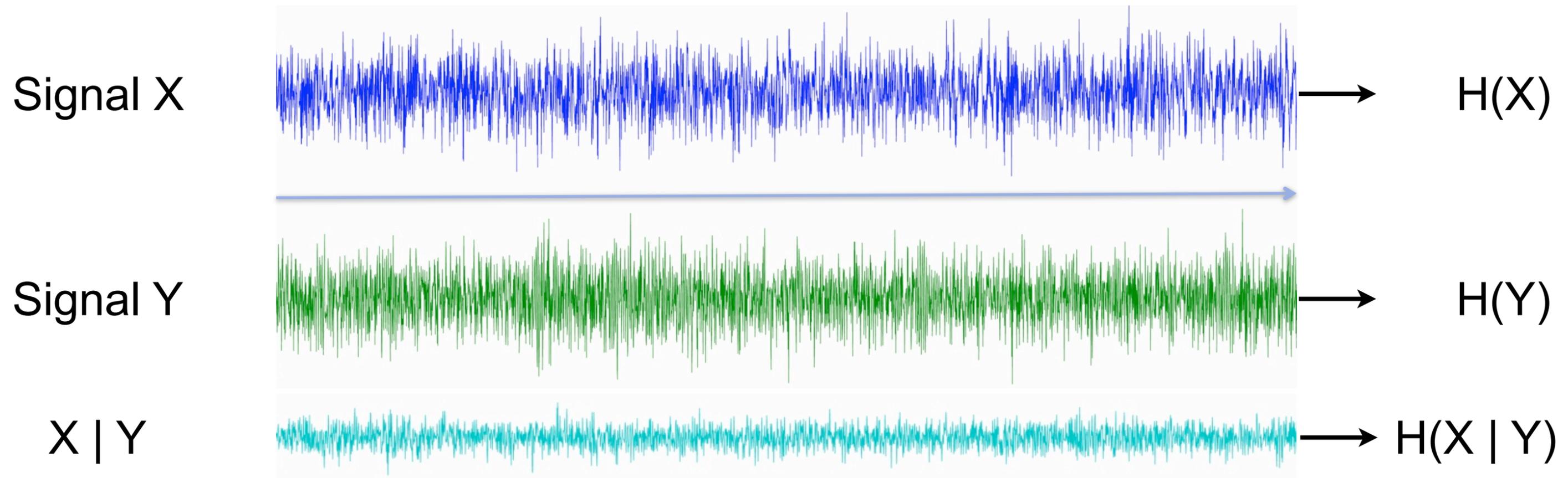
Conditional  
Entropy

Mutual  
Information

Schreiber 2000

# Transfer Entropy

Mutual Information



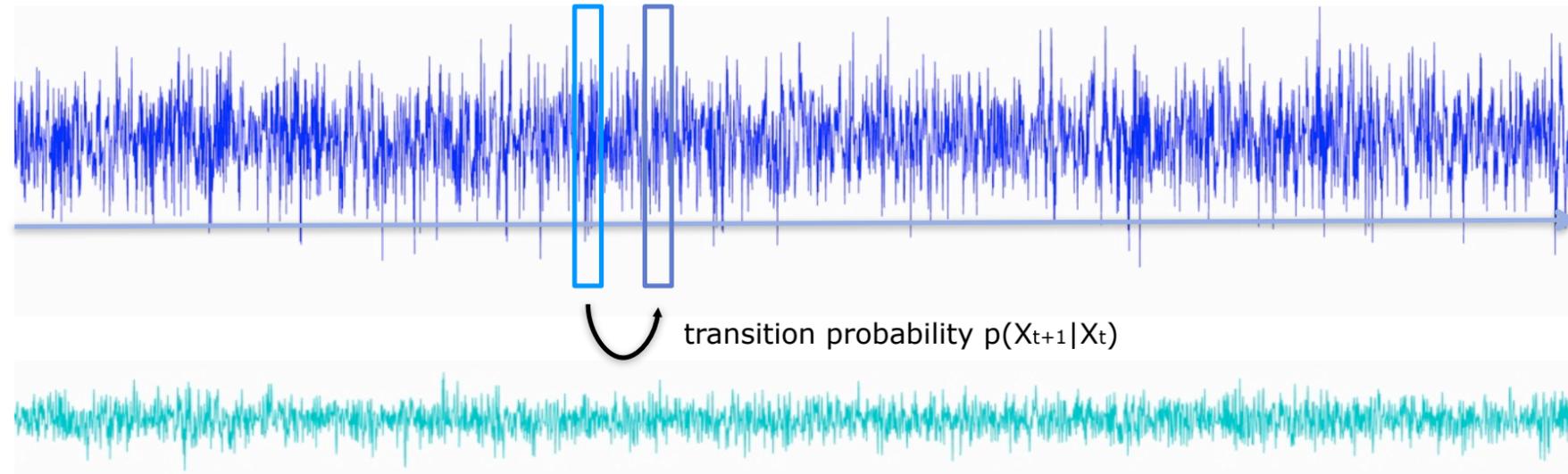
$$I(X, Y) = H(X) + H(Y) - H(X|Y)$$

“Mutual information”

# Transfer Entropy

## Conditional Entropy

Conditional Entropy:  $H(X_{t+1}|X_t)$



Mutual information:  $I(X, Y)$

“Apparent Transfer entropy”

Conditional mutual information:  $I(X, Y_{t+1}|Y_t)$

“Conditional transfer entropy”

predictive information:  $H(X_{t+1})$  -  $H(X_{t+1}|X_t)$

total uncertainty  
about the future

uncertainty  
about the future,  
given the past

Full length implementation formulas:

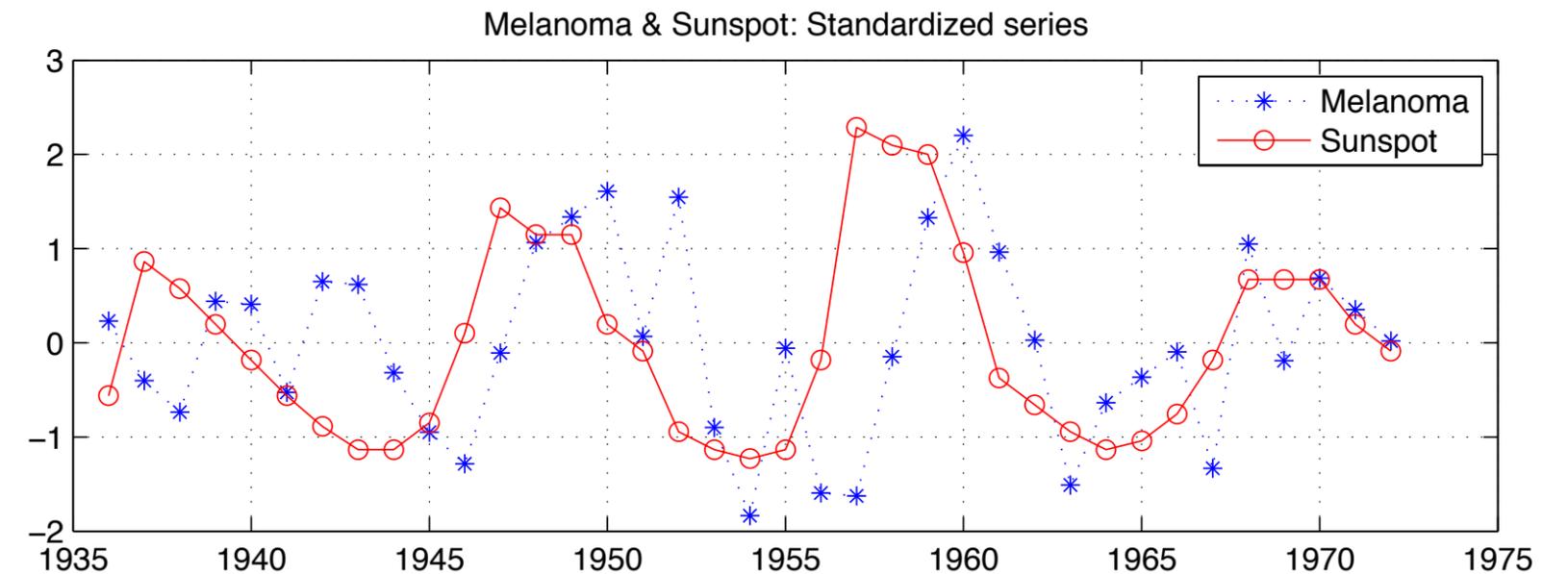
$$T_{J \rightarrow I} = \sum_{x_{n+1}, x_n, y_n} p(x_{n+1}, x_n, y_n) \log \left( \frac{p(x_{n+1}, x_n, y_n) \cdot p(x_n)}{p(x_n, y_n) \cdot p(x_{n+1}, x_n)} \right)$$

$$T_{I \rightarrow J} = \sum_{y_{n+1}, x_n, y_n} p(y_{n+1}, x_n, y_n) \log \left( \frac{p(y_{n+1}, x_n, y_n) \cdot p(y_n)}{p(x_n, y_n) \cdot p(y_{n+1}, y_n)} \right)$$

# Properties of Transfer Entropy

## Advantages

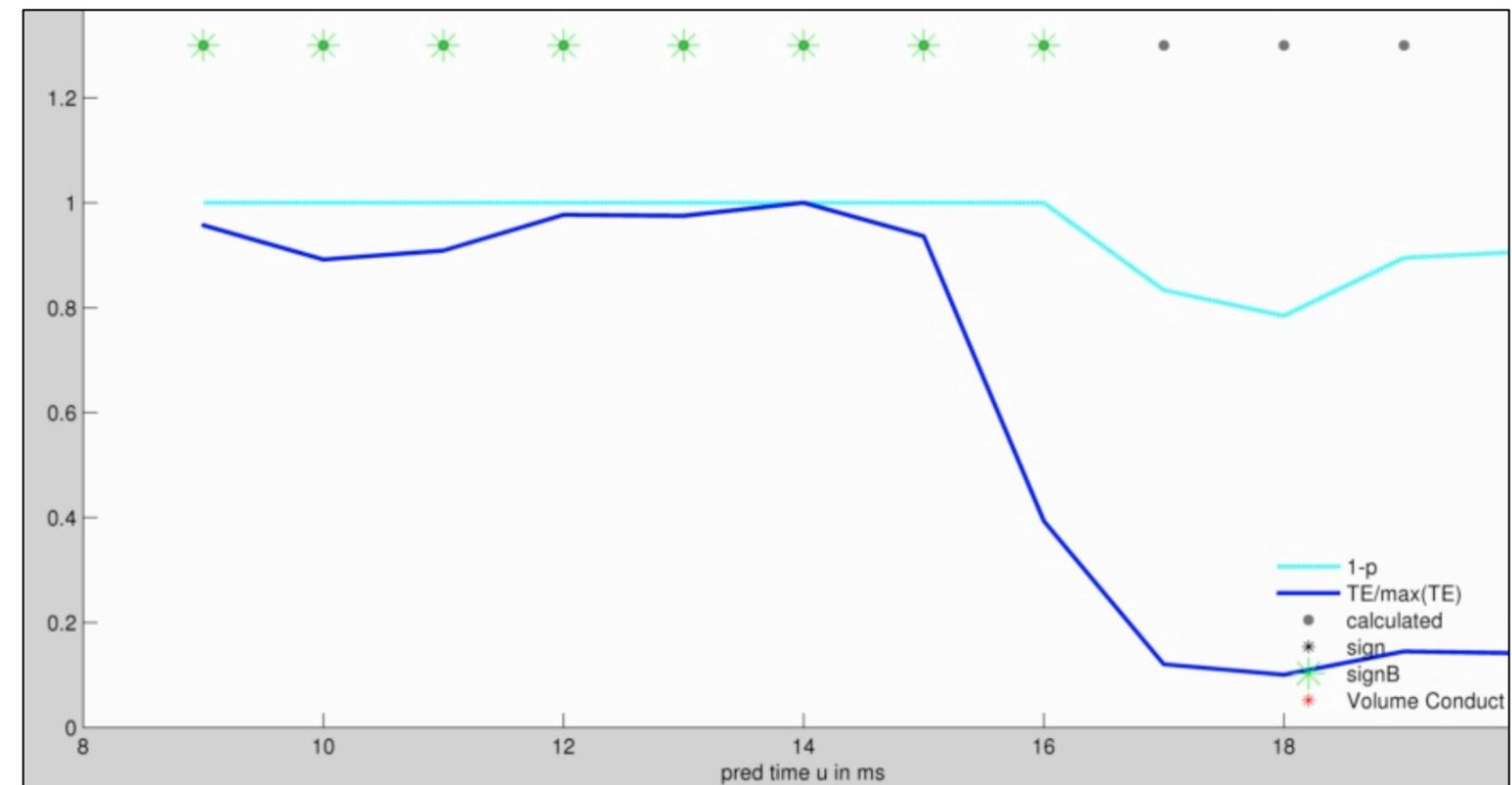
- model-free
- robust to noise
- inherently non-linear
  - but works fast with linear data
- weaker coupling -> better results!
- copes well with multivariate effects:  $\bigcirc \rightarrow \triangle \rightarrow \square \neq \bigcirc \rightarrow \square$



# Properties of Transfer Entropy

## Application in Neuroscience

- causal interactions occur at a fine temporal scale ( $<10\text{ms}$ )
- (predictable) estimation bias for non-infinite data sequences
- Noise influence:
  - good detection rate for SNR above 15db
  - breaks down to 50% at 10db
- Issues with complex networks
- difficult to test for significance
- vulnerable to volume conduction



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